Multiplication Curriculum



Woodland Grange Primary School

Aiming high to achieve excellence and success by working together.

Understanding the operation and related vocabulary.

Mental Calculations

Written Calculations

Understanding the operation

Begin to understand multiplication by using concrete objects, pictorial representations and arrays to solve problems; make connections between the different representations.

begin to use the vocabulary involved in multiplying

Vocabulary

ones, groups, lots of, doubling repeated addition array, row, column, groups of, lots of, times, columns, rows longer, bigger, higher etc times as (big, long, wide ...etc)

Generalisations

Understand 6 counters can be arranged as 3+3 or 2+2+2

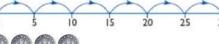
Understand that when counting in twos, the numbers are always even.

Some Key Questions Why is an even number an even number? What do you notice? What's the same? What's different? Can you convince me? How do you know? Number facts Count in multiples of twos, fives and tens 0 2 4 6 8 10...



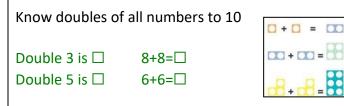
How many legs have 5 teddies got altogether?

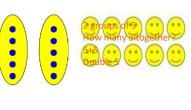




How much money have I got in my purse? 5,10,15,20

How many 10ps do I need to buy a chocolate bar for 30p?

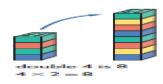




No formal written layout.

Children will be recording their mathematics using pictorial representations, arrays, number lines and mathematical statements.





Begin to recognise odd and even numbers Use cubes to make 9 and recognise it is odd (as the cubes cannot be paired)

Sort Numicon into odd and eve numbers



What happens if we out two odd numbers together? Mental Methods and jottings

Counting

Count a set of objects by grouping in 2s, 5s or 10s Count these marbles (2 at a time)



Solve problems involving doubling and equal groups I need 5 eggs to bake a cake. How many eggs will I need to bake 2 cakes?

Counting on

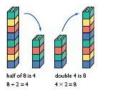
There are 3 pots. Each pot has 2 seeds in. How many seeds are planted?

(by counting on in twos using objects or pictures to keep track)

Doubling and halving

A ladybird has 6 spots on each wing. How many spots are there altogether? (by recognising 6+6=12)





Mental Calculations

How many sides have these triangles

40

got altogether? 3,6,9,12

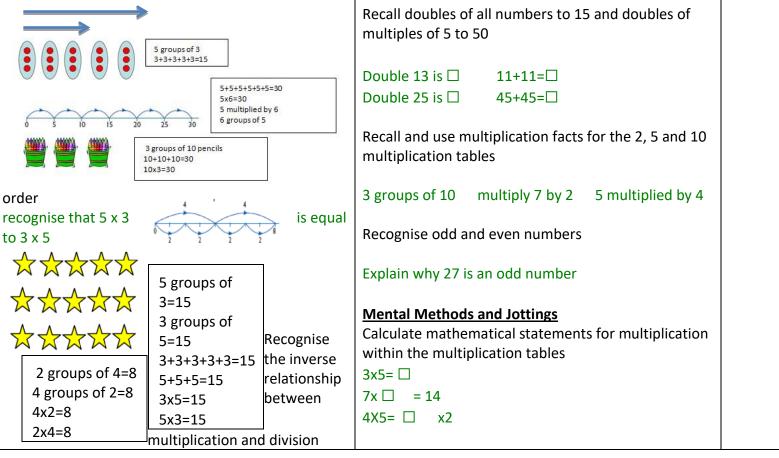
Understanding the operation and related vocabulary.

Understanding the operation

Understand multiplication as

- repeated addition
- describing an array
- scaling (to compare 2 items) e.g. twice as long
- correspondence problems one to many

Show that multiplication of two numbers can be done in any



Number facts

Count in steps of 2, 3, and 5 from 0

0369121518.....30

50 45 40 35 30 0

Which numbers do you need to add to the counting stick?

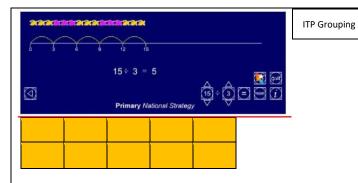
20

25

No formal written layout. Children will be recording their mathematics using pictorial representations, arrays, number lines and mathematical statements.

Written Calculations

See jottings in other columns.



Write the related number sentences 5x2=10 2x5=10 10=5x2 10=2x5 10÷2=5 10÷5=2 2=10÷5 5=10÷2

Write mathematical statements using the multiplication (×), and equals (=) signs 5x4=20 16=8x2 $3x\Box=15$ $\Box=2x7$ 20= $\Box x\Box$

<u>Vocabulary</u>

multiple, multiply, multiplication array, multiplication tables / facts, groups of, lots of, times, columns, rows, once, twice, three, ten...times a big, repeated addition

Generalisation

Repeated addition can be shown mentally on a number line

Inverse relationship between multiplication and division. Use an array to explore how numbers can be organised into groups.

Some Key Questions

What do you notice? What's the same? What's different? Can you convince me? How do you know?

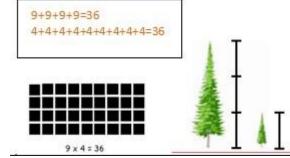
Counting on 7x5 (by counting on in fives using fingers to keep track)	
With jottings 3x5 (by counting on in threes using a number line to keep track)	
Doubling and halving 7x2 (by recalling the doubles fact)	
With jotting 12x2 (by doubling 10, doubling 2 and recombining)	
12	
double \checkmark	
20	
24	
Estimating and Checking Begin to use equivalent calculations to check answers	

Understanding the operation and related vocabulary.

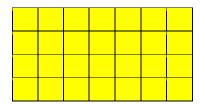
Understanding the operation

Understand multiplication as

- repeated addition
- describing an array
- Scaling comparison and enlargement
- correspondence problems one to many and many-tomany



Understand commutativity and associativity recognise that 7x4 is equal to 4x7



recognise that if calculating 2x3x10 the numbers can be combined in any order

Understand the inverse relationship between multiplication and division write the related number sentences $6x3=18\ 3x6=18\ 18=6x3\ 18=3x6$ $18\div3=6\ 18\div6=3\ 3=18\div6\ 6=18\div3$

Mental	Calculations

Number facts

Count from 0 in multiples of 4, 8, 50 and 100 0 8 16 24 32 500 450 400 350



Recall doubles of all numbers to 20, doubles of multiples

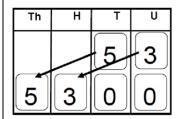
of 5 to 100 and doubles of multiples of 100 to 500 $\,$

Double 17 is 🗆	19x2=□
Double 65 is 🗆	85x2=□
Double 300 is 🗆	400+400=□

Recall and use multiplication facts for the 3, 4 and 8 multiplication tables and begin to use knowledge of place value to derive related facts

3 groups of 8 the product of 8 and 4

multiply 9 by 4 d 4 50 multiplied by 4

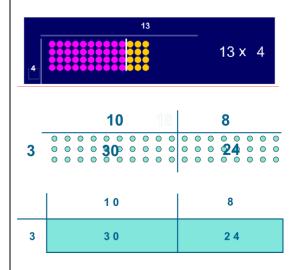


<u>Place value cards</u> Use digit cards to make numbers in the grid. Show how each digit in a number moves one column to the left when a number is multiples by 10 and two columns to the left when a number is multiplied by 100.

Written Calculations

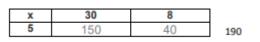
Begin to use formal written methods for two-digit numbers multiplied by one-digit numbers (multiplication facts)

Use models and images to demonstrate grid method



Give children opportunities for children to explore this and deepen understanding using manipulatives such as Dienes apparatus and place value counters

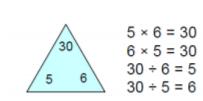
38x5



*Children to use grid method by the end of year 3

Mental Methods and Jottings

Calculate mathematical statements for multiplication



Solve missing numbers problems involving multiplication

Trio cards

3x□=15 □=2x7 20=□x□ 25 + 10 = 5 x□ 15<□ x 2□x□> 20 Vocabulary

partition, grid method, inverse, product

Generalisations

Connecting x2, x4 and x8 through multiplication facts

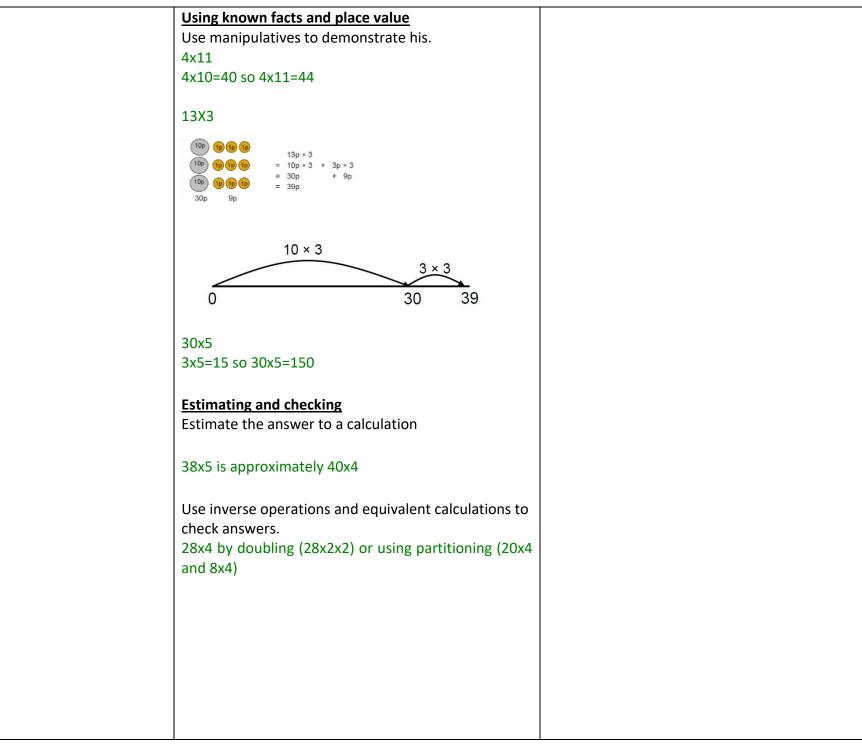
Comparing times tables with the same times tables which is ten times bigger. If $4 \times 3 = 12$, then we know 4 x 30 = 120. Use place value counters to demonstrate this.

When they know multiplication facts up to x12, do they know what x13 is? (i.e. can they use 4x12 to work out 4x13 and 4x14 and beyond?)

Some Key Questions

What do you notice? What's the same? What's different? Can you convince me? How do you know?

using the multiplication tables that they know,	
including for two-digit numbers times one-digit	
numbers	
Use doubling to connect 2, 4 and 8 multiplication	
tables	
Counting on	
5x14 (by counting on in fives from 50)	
with jottings	
4x13 (by counting on in fours from 4x10 using a	
number line to keep track)	
4x10 4x13=52	
0 40 44 46 52	
Doutioning (with distributive law)	
Partioning (with distributive law)	
Without crossing the tens boundary 32x3= (30x3=90, 2x3=6,	
90+6=96)	
5010=50)	
10 7	
with jottings	
Crossing the tens boundary	
17x5= (10x5=50, 7x5=35,	
50+35=85)	
Doubling and halving	
0x20 (multiply by 10 and 28 56	
9x20 (multiply by 10 and 7 7 7 then double)	
9x10=90 Double 90 is 180	
56 112	
with jottings	
28x4 (double and double again)	
Double 28 is 56, double 56 is 112	
7	



Mental Calculations

Understanding the operation and related vocabulary.

Understanding the operation

Continue to understand multiplication as

- repeated addition
- describing an array
- scaling comparison and enlargement
- correspondence problems one to many and manyto-many

11+11+11+11=44 7+7+7+₇₊₇₊₇₊₇₌₄₉

Understand the distributive law

recognise that 14x5 is the same as 10x5 added to 4x5

19 x 5 = (9 x 5) + (10 x 5) = 45 + 50 = 95 36 x 9 = (30 x 9) + (6 x 9) = 270 + 54 = 324

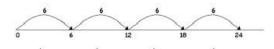
continue to understand commutativity and associativity

 Number facts

 Count in multiples of 6, 7, 9, 25 and 1000

 0 7 14 21 28 ...

 300 275 250 225 200 ...







325

375

ITP Number Grid

Derive doubles of multiples of 50 to 1000 and multiples of 1000

 Double 950 is □
 750x2=□

 Double 8000 is □
 6000+6000=□

Recall multiplication facts for multiplication tables up to 12×12 , and use place value to derive related facts

7 groups of 8 multiply 9 by 6 the product of 8 and 11 60 multiplied by 4

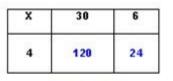
Recognise factor pairs list the factors pairs of 32

Written Calculations

Multiply two-digit and three-digit numbers by a one-digit number using formal written layout

Children to embed and deepen their understanding of the grid method to multiply. Ensure this is still linked back to their understanding of arrays and place value counters.

36 x 4 = 144

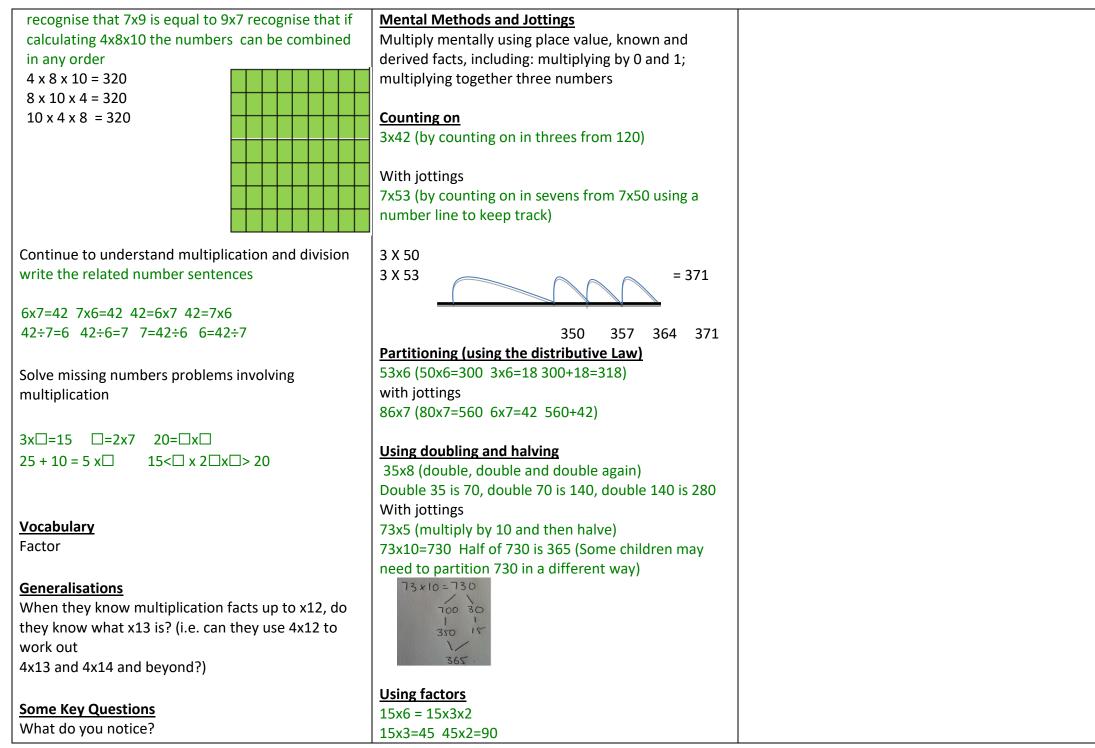


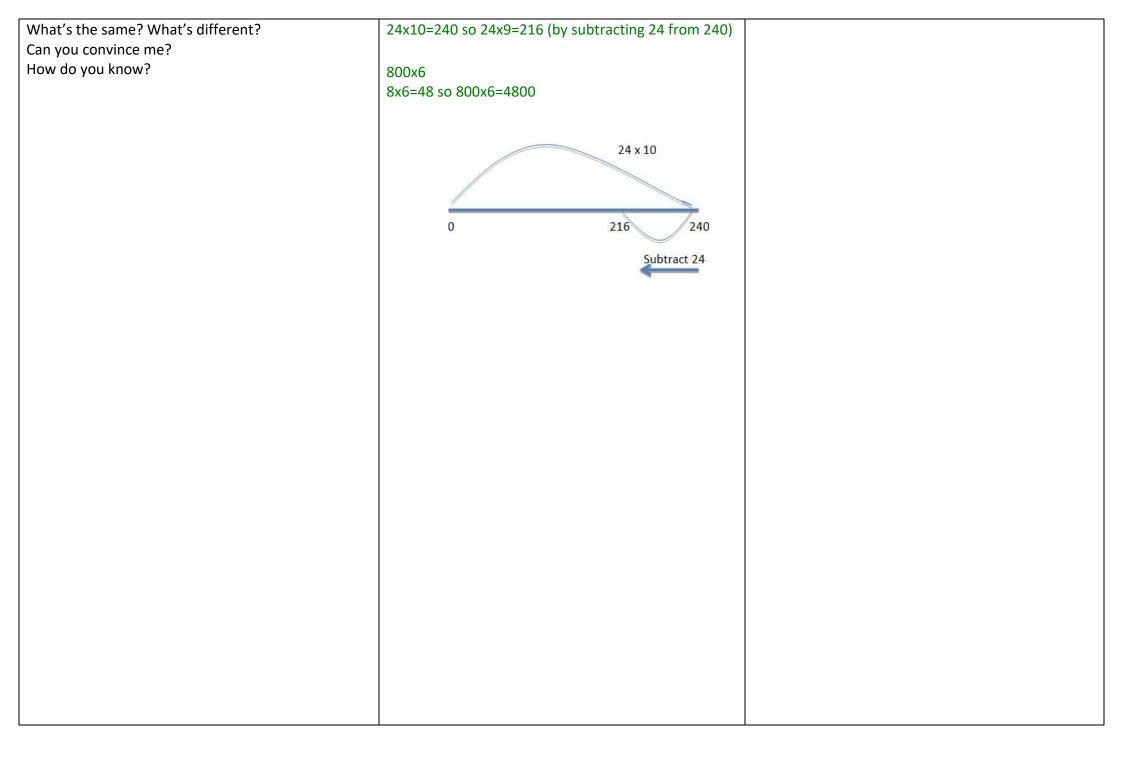
120 + 24 = 144 (add the partial products)

127 x 6 = 762

x	100	20	7
6	600	120	42

600 + 120 + 42 = 762 (add the partial products)





Asutal Calculation

Understanding the operation and related vocabulary.

Understanding the operation

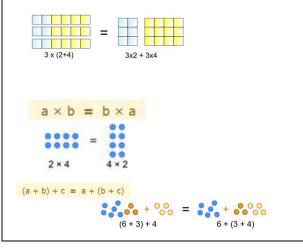
Continue to develop understanding of multiplication to include:

- scaling by simple fractions
- simple rates



Continue to understand the distributive, commutative and associative laws recognise that 37x6 is the same as 30x6 added to 7x6

(distributive) recognise that 25x7 is equal to 7x25 (commutative) recognise that if calculating 18x4x10 the numbers can be combined in any order (associative)



Mental Calculations				
<u>Number facts</u>				
Use knowledge of counting in multiples to				
count in decimal steps (one decimal place) 0.6				
1.2 1.8 2.4				
8.4 7.7 7.0 6.3				

Derive doubles of decimals (to one decimal place) using knowledge of place value

 Double 0.4 is □
 0.7x2=□

 Double 3.8 is □
 5.6+5.6=□

Continue to recall multiplication facts for multiplication tables up to 12×12 fluently, and derive and use related facts

7 groups of 8multiply 12 by 9the product of 80 and 400.6 multiplied by 4x 1 2 3 4 5 6 7 8 9 30 11 12

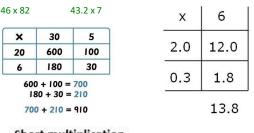


Identify multiples and factors, and common factors of two numbers. list the factors of 96 identify the common factors of 30 and 36 by listing factor pairs give a number that is a multiple of 3 and a multiple of 2 (and recognise these are multiples of 6) list the multiples of 9 between 150 and 180 (using tests of divisibility)

Written Calculations

Multiply numbers up to 4 digits by a one- or twodigit number using a formal written method, including long multiplication for two-digit numbers. Multiply numbers with up to one decimal place by onedigit whole number.

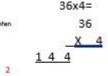
Use grid method, progressing to short and long multiplication for numbers with more digits only when children have secure understanding of multiplication facts and place value. Continue to embed understanding through the use of manipulatives and grid method. <u>Grid method</u>



Short multiplication

144





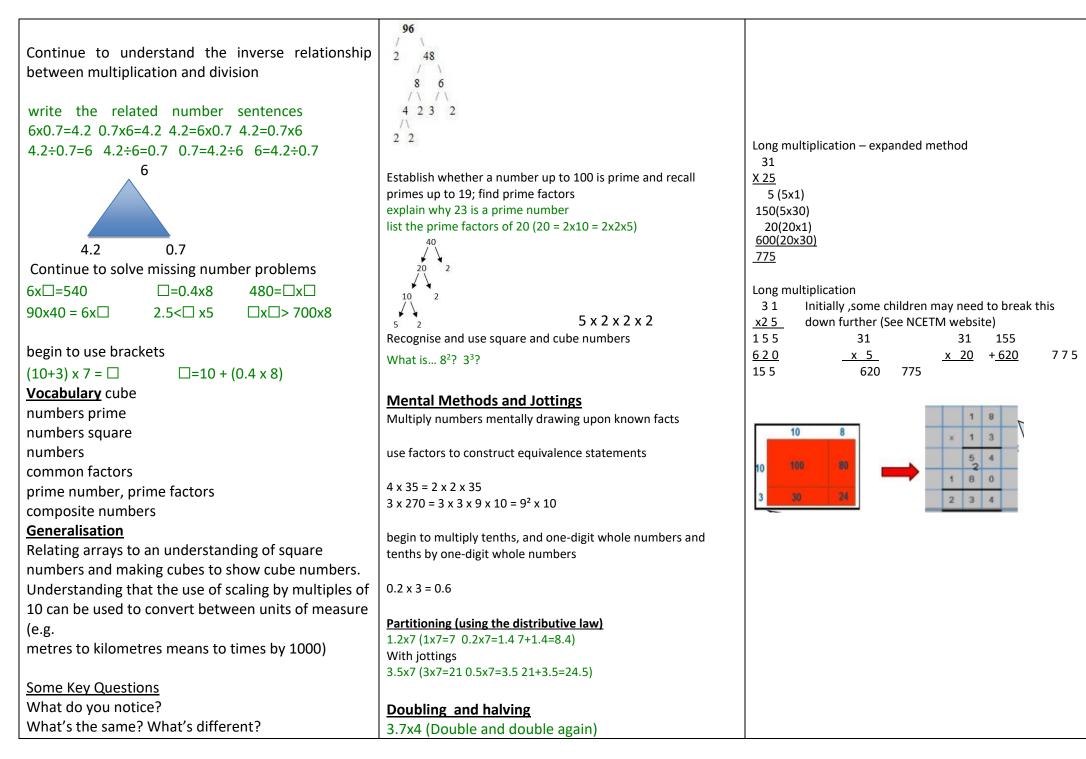
Short multiplication for multiplying by a single digit

32

3.0



Papils could be asked to work out a given calculation using the grid, and then compare it to 'your' column method. What are the similarities and differences? Unpick the steps and show how it reduces the steps.



Can you convince me?	Double 3.7 is 7.4, double 7.4 is 14.8	
How do you know?	with jottings	
	76x50 (multiply by 100 and halve)	
	76x100=7600 Half of 7600 is 3800	
	Heine factors	
	Using factors 25x12=25x2x6	
	25x2=50 50x6=300	
	with jottings	
	3x270=3x3x9x10	
	3x3x9=9 ² 9 ² =81 81x10=810	
	5,5,5,5-5 5 -61 61,10-610	
	Using Known facts and place value	
	Using Known facts and place value 13x19	
	13x20=260 so 13x19=247 (subtract 26 from 260)	
	13x20-200 30 13x19-247 (30btract 20 11011 200)	
	3x14	
	recognise 3x14 is equivalent to 6x7	
	Fatimatics and Charling	
	Estimating and Checking	
	Check 86x9 by using an equivalent calculation	
	Multiply by 10 and adjust (860-86) or partition (80x9 added to 6x9)	

	MULTIPLICATION: Y6						
Understanding the operation and related vocabulary.	Mental Calculations	Written Calculations					
 Understanding the operation Continue to understand Scaling by fractions Of the 90 students on a field trip to the zoo, two ninths want to go to see the bears. How many students want to see the bears? 90÷ 2/9 90÷9 = 10 10 X 2 = 20 Rate A car travels 60 miles per hour. How far will it travel in 2 and a quarter hours? 	Number factsUse knowledge of counting in multiples to count in decimal steps (two decimal places) $0.09 \ 0.18 \ 0.27 \ 0.36 \$ $0.48 \ 0.44 \ 0.4 \ 0.36 \$ Derive doubles of decimals (to two decimal places)using knowledge of place valueDouble 0.47 is \Box $0.73x2=\Box$ Double 3.08 is \Box $2.59+2.59=\Box$	digit wh of long r Multiply	ole numb multiplicat numbers and two- ETHOD 3	er using th tion	ne formal o two dec	digits by a written me imal place	ethod
Use their knowledge of the order of operations - BODMAS Understand that when there are no brackets in an expression, do multiplication or division before addition or subtraction Understand that if the operations are at the same level of priority, work out the example from left to right Continue to solve missing number problems 6x = 0.54 $= 0.06x8$ $4.8 = x = 100000000000000000000000000000000$	Continue to recall multiplication facts for multiplication tables up to 12×12 fluently, and derive and use related facts 30 multiplied by 800 multiply 0.12 by 6 the product of 0.08 and 4 0.4 multiplied by 0.5 + identify common factors, common multiples and prime numbers find the highest common factor of 18 and 24 find the lowest common multiple of 6 and 15 identify whether 87 is a prime number list the prime factors of 84 (84 = $2x42 = 2x2x21 = 2x2x3x7$) use the tests of divisibility to identify factors and multiples continue to use square and cube numbers What is12 ² ? 6 ³ ?	shown b mental a multiplia Value (s Develop	elow unti calculation cation tab see year 5	click between digits to a linsert or remove a decimal point of be taug they are n strategie les and the pethods wi	thorough es, recall c e applicat	31.5 Click the hidd or decrease t click to hidd show the num above this bill clowing met by secure w of clon of Place	rrasse his digit or mber atton
Generalisations	Mental Methods and Jottings						

Order of operations: brackets first, then	Perform mental calculations, including with mixed	1234	3652	
multiplication and division (left to right) before	operations, large numbers and decimals	× 16	* 8	
addition and subtraction		7404 (1234×6) 12340 (1234×10)	29,216	
(left to right). Children could learn an acrostic to	Partitioning (using distributive law)	19,744		
remember this or could be encouraged to design	6.04x3 (6x3=18 0.04x3=0.12 18+0.12=18.12)			
their own ways of remembering.	With jottings			
Understanding the use of multiplication to support	0.43x6 (0.4x6=2.4 0.03x6=0.18 2.4+0.18=2.58)			
conversions between units of measurement.				
	Doubling and halving			
Some Key Questions What	0.24x40 (double and double again, then multiply by			
do you notice?	10)			
What's the same? What's different?	Double 0.24 is 0.48, double 0.48 is 0.96, 0.96x10=9.6			
Can you convince me?				
How do you know?	With jottings			
	68x25 (multiply by 100, then halve and halve again)			
	68x100=6800 Half of 6800 is 3400 Half of 3400 is			
	1700			
	Using factors			
	1.5x16=1.5x2x8			
	1.5x2=3 3x8=24			
	with jottings 32x24 = 32x3x8			
	32x3=96 96x8=800-(4x8)=768			
	Using known facts and Place value			
	17x98			
	17x100=1700 so 17x98 is 1666 (subtract 17x2 from			
	1700)			
	1,001			
	15x18			
	recognise 15x18 is equivalent to 30x9			
	Estimating and checking			

Use estimation to check answers to calculations and determine, in the context of a problem, levels of accuracy. 5872x54 is approximately 6000x50	
Continue to use appropriate strategies to check answers Check 496x5 by using an equivalent calculation Multiply by 10 and halve or use a known fact and adjust (500x5) –(4x5)	